Exercise 4

Task 1 (Nondeterministic Logspace). A cycle in a directed graph is a path v_1, \ldots, v_n , such that $v_1 = v_n$ and $v_i \neq v_j$ for all other nodes v_i and v_j . A directed graph is called *acyclic*, if it does not contain a cycle. Does the problem ACYCLIC

Input: A directed graph G = (V, E). **Question:** Is G acyclic? belong to the complexity class **NL**?

Task 2. Let

$$\mathbf{EXP} = \bigcup_{k \in \mathbb{N}} \mathbf{DTIME}(2^{n^k}) \text{ and } \mathbf{NEXP} = \bigcup_{k \in \mathbb{N}} \mathbf{NTIME}(2^{n^k}).$$

Prove the following statement by using the padding technique: If $\mathbf{P} = \mathbf{NP}$, then also $\mathbf{EXP} = \mathbf{NEXP}$.

Task 3. Show that NL = coNL is equivalent to the theorem of Immerman and Szelepcsényi.