

Exercise 9

Task 1

Let $f, g \in \mathbb{R}[x]$ with

$$\begin{aligned}f(x) &= x^4 + x^3 - x - 1, \\g(x) &= 4x^3 + 3x^2 - 1.\end{aligned}$$

Compute the Sturm sequence $[f, g]$.

Task 2

Compute the number of zeros of $f(x) = x^4 - x^2 - 1$ in the interval $(-2, 2)$ using the Theorem of Sturm and Tarski.