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Lehrstuhl Theoretische Informatik
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Exercise 7

Task 1
Find the optimal order to compute the following product (only the dimensions of the matrices are given):

$$(2 \times 4) \cdot (4 \times 6) \cdot (6 \times 1) \cdot (1 \times 10) \cdot (10 \times 10)$$

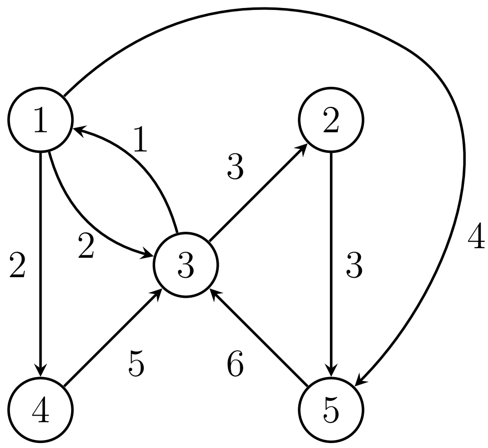
Task 2
Let $X = (x_1, \ldots, x_m)$ and $Y = (y_1, \ldots, y_n)$ be two sequences. We say X is a *subsequence* of Y if there are indices $1 \leq i_1 < i_2 < \cdots < i_m \leq n$ such that for all $1 \leq j \leq m$ it holds that $x_j = y_{i_j}$.
Use dynamic programming to implement an algorithm that runs in polynomial time which, given two sequences X and Y, computes the length of the longest common subsequence of X and Y.

Task 3
Construct an optimal binary search tree for the following elements v with probability (weight) $\gamma(v)$.

v	1	2	3	4	5	6
$\gamma(v)$	0.25	0.1	0.2	0.15	0.25	0.05

Task 4
Assume we want to construct an optimal binary search tree using the following greedy algorithm: Choose an element v for which $\gamma(v)$ is maximal as the root node and then continue recursively. Show that this approach does not always yield an optimal binary search tree.

Task 5
Use Floyd's algorithm to compute all shortest paths in the following graph: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