## **Exercise 4**

**Task 1** (Nondeterministic Logspace). A cycle in a directed graph is a path  $v_1, \ldots, v_n$ , such that  $v_1 = v_n$  and  $v_i \neq v_j$  for all other nodes  $v_i$  and  $v_j$ . A directed graph is called acyclic, if it does not contain a cycle. Does the problem ACYCLIC

**Input:** A directed graph G = (V, E).

Question: Is G acyclic?

belong to the complexity class **NL**?

Task 2. Let

$$\mathbf{EXP} = \bigcup_{k \in \mathbb{N}} \mathbf{DTIME}(2^{n^k}) \text{ and } \mathbf{NEXP} = \bigcup_{k \in \mathbb{N}} \mathbf{NTIME}(2^{n^k}).$$

Prove the following statement by using the padding technique: If P = NP, then also EXP = NEXP.

**Task 3.** Show that NL = coNL is equivalent to the theorem of Immerman and Szelepcsényi.